

FORMULAE

SLR

- $\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}$
- $\hat{\beta}_1 = \frac{S_{xy}}{S_{xx}}$
- $s^2 = \frac{SSE}{n-2}$ $SSE = S_{yy} - \frac{(S_{xy})^2}{S_{xx}}$ $S_{xx} = \sum x_i^2 - \frac{(\sum x_i)^2}{n}$
- $t = \frac{\hat{\beta}_1}{s/\sqrt{S_{xx}}} \sim t_{(n-2)}$ $S_{yy} = \sum y_i^2 - \frac{(\sum y_i)^2}{n}$
- $100(1-\alpha)\%$ C.I. for $\beta_1 : \left(\hat{\beta}_1 \pm t_{\alpha/2; n-2} \cdot \frac{s}{\sqrt{S_{xx}}} \right)$ $S_{xy} = \sum x_i y_i - \frac{(\sum x_i)(\sum y_i)}{n}$
- $TSS = S_{yy}$ $SSR = \frac{(S_{xy})^2}{S_{xx}}$ $F = \frac{MSR}{MSE} \sim F_{(1, n-2)}$
- $100(1-\alpha)\%$ C.I. for $E(y | x_p) : \left(\hat{y} \pm t_{\alpha/2; n-2} \cdot \sqrt{MSE \left(\frac{1}{n} + \frac{(x_p - \bar{x})^2}{S_{xx}} \right)} \right)$
- $100(1-\alpha)\%$ P.I. for individual $y | x_p : \left(\hat{y} \pm t_{\alpha/2; n-2} \cdot \sqrt{MSE \left(1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{S_{xx}} \right)} \right)$
- coefficient of correlation between x & y : $r = \frac{S_{xy}}{\sqrt{S_{xx} S_{yy}}}$
- coefficient of determination: $r^2 = \frac{SSR}{TSS}$
- lack of fit: $SSE = SSPE + SSLF$, $SSPE = \sum_i \sum_j (y_{ij} - \bar{y}_i)^2$

$$F_{LF} = \frac{MSSLF}{MSSPE} = \frac{SSLF / [n-2 - \sum (n_i - 1)]}{SSPE / [\sum (n_i - 1)]} \sim F_{(n-2 - \sum (n_i - 1), \sum (n_i - 1))}$$