

Lab #4.

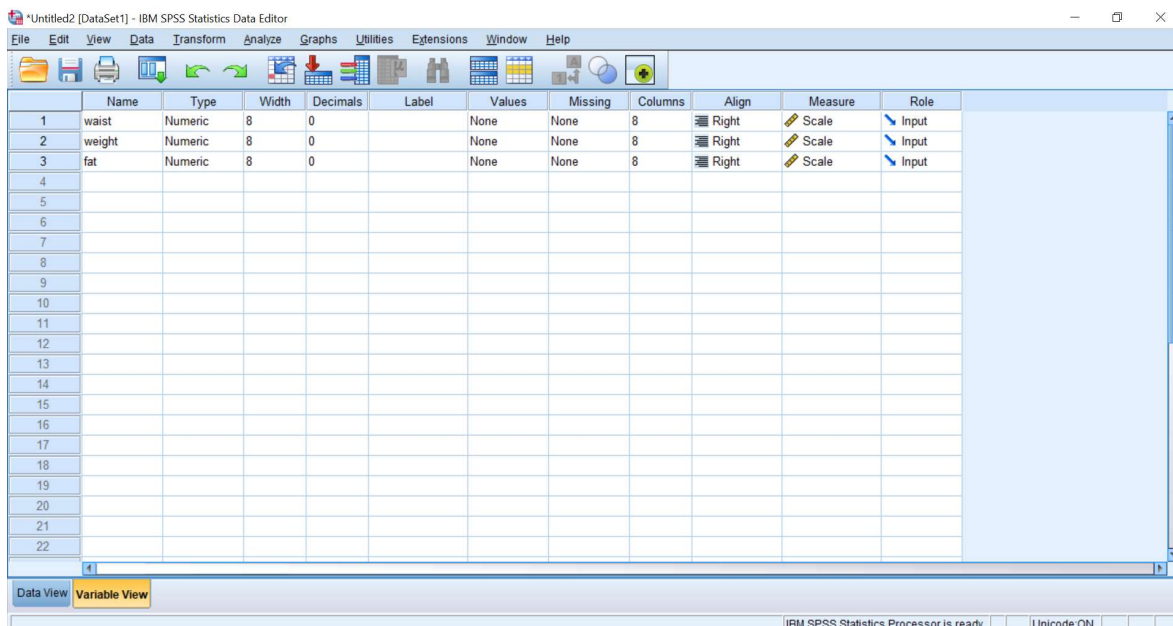
Body fat, waist and weight_MLR Ex.

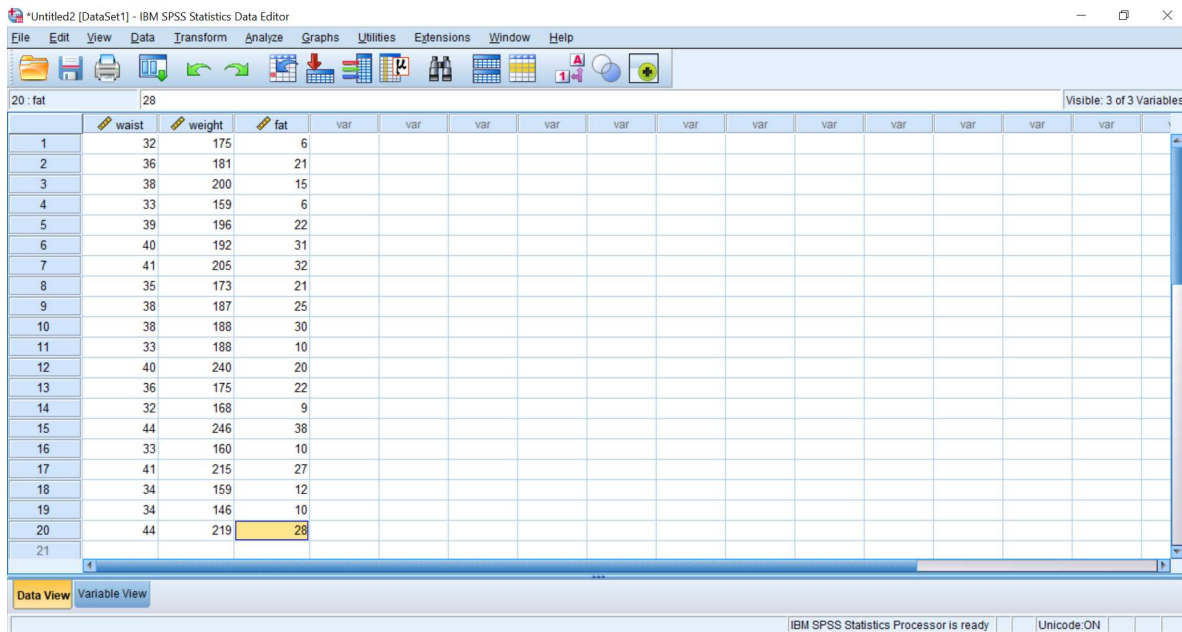
The following table gives the waist size (in inches), weight (in pounds) and the body fat (in %).

Waist (X_1)	Weight (X_2)	Body Fat (Y)
32	175	6
36	181	21
38	200	15
33	159	6
39	196	22
40	192	31
41	205	32
35	173	21
38	187	25
38	188	30
33	188	10
40	240	20
36	175	22
32	168	9
44	246	38
33	160	10
41	215	27
34	159	12
34	146	10
44	219	28

Consider the model $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \varepsilon$.

Enter the data





To obtain the residuals and predicted values, go to “Analyze” → “Regression” → “Linear” → click on “save” and select “Unstandardized Predicted values” and “Unstandardized residuals”. Then click “continue” . After clicking on “OK” you will get ANOVA table with all the parameter estimates.

Regression

Variables Entered/Removed^a

Model	Variables Entered	Variables Removed	Method
1	weight, waist ^b	.	Enter

a. Dependent Variable: fat

b. All requested variables entered.

Model Summary^b

Model	R	R Square	Adjusted R Square	Std. Error of the Estimate
1	.894 ^a	.800	.776	4.526

a. Predictors: (Constant), weight, waist

b. Dependent Variable: fat

ANOVA^a

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	1389.491	2	694.746	33.913	.000 ^b
	Residual	348.259	17	20.486		
	Total	1737.750	19			

a. Dependent Variable: fat

b. Predictors: (Constant), weight, waist

Coefficients^a

Model		Unstandardized Coefficients		Standardized	t	Sig.
		B	Std. Error	Beta		
1	(Constant)	-65.074	10.406		-6.254	.000
	waist	2.689	.521	1.074	5.163	.000
	weight	-.079	.075	-.219	-1.053	.307

a. Dependent Variable: fat

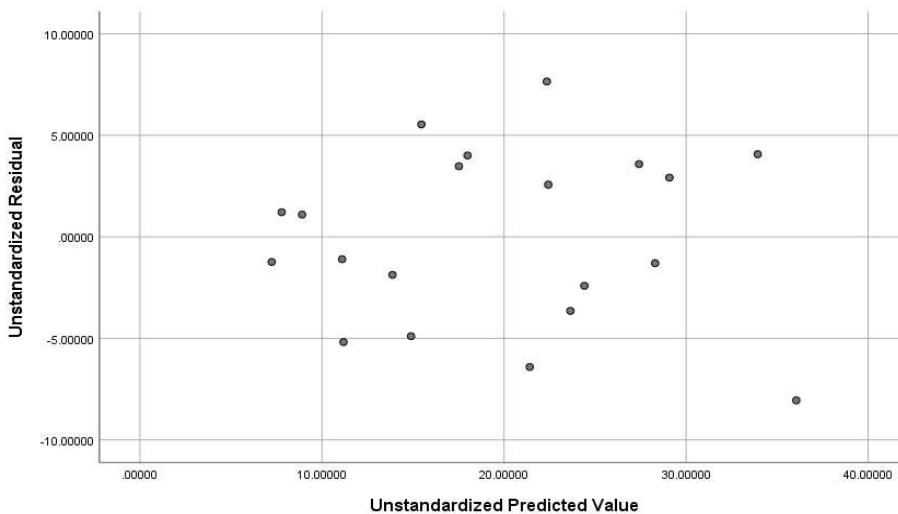
$\hat{\beta}_1$

$\hat{\beta}_0$

$\hat{\beta}_2$

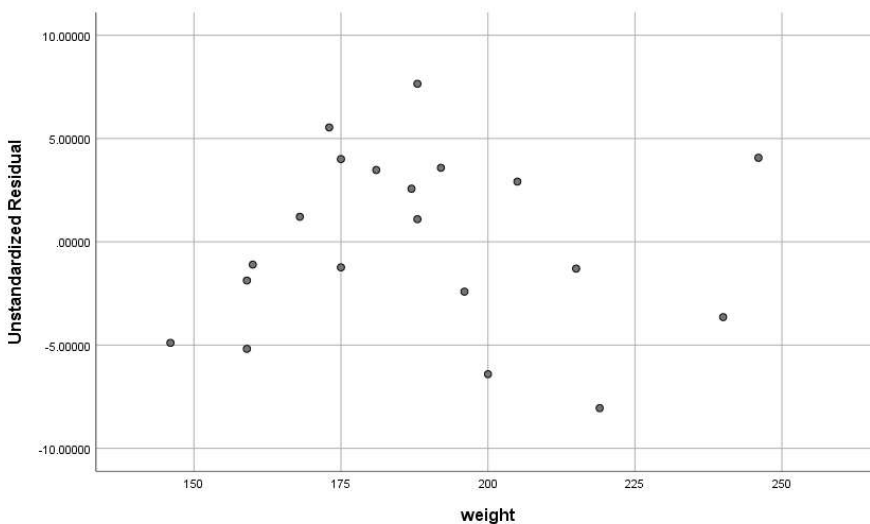
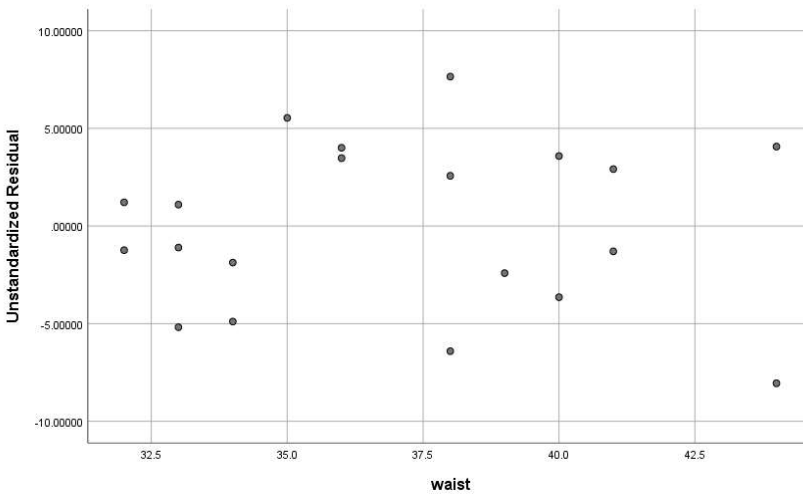
Residual Analysis:

plot of predicted values vs residuals (i.e. \hat{y}_i vs e_i) → “graph” → “Legacy Dialog” → “scatter/dot”
 → “Simple scatter” → “Define” → put “Residuals” on the y axis and “Predicted Values” on the x axis
 → OK (this is to verify the **assumption of independence of the errors**)

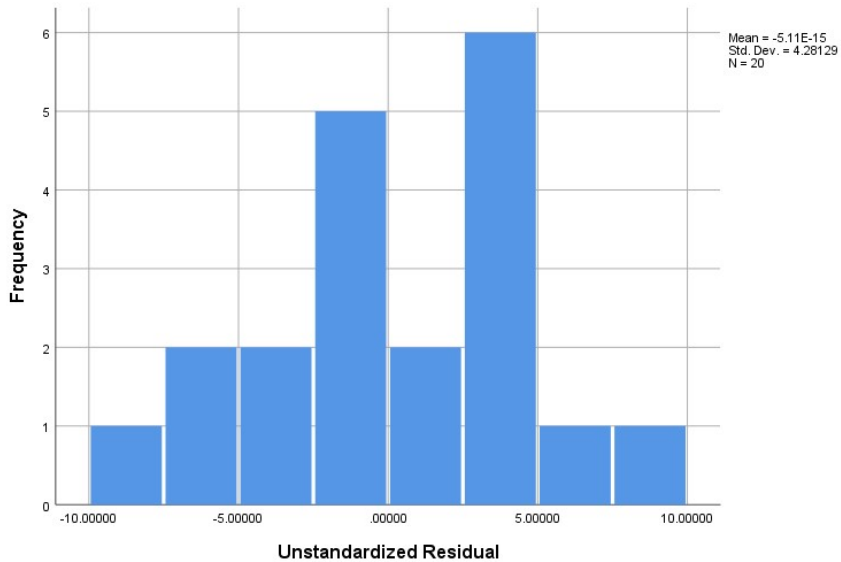


To obtain the **plot of x's vs residuals (i.e x_i vs e_i)** → “graph” → “Legacy Dialog” → “scatter/dot” → “Simple scatter” → “Define” → put “Residuals” on the y axis and “waist” on the x axis → OK

And repeat with “weight” (to verify the **assumption of constant variance for every x**, we need to plot x_1 vs residuals and x_2 vs residuals)



To obtain the **histogram of the errors** → “Graphs” → “Legacy Dialogs” → “Histogram” → select Unstandardized Residuals as a response variable and then click OK



To do F_{drop} or F_{part} test, we need to obtain ANOVA table for the reduced model.

Our Full model is $y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \varepsilon$, ANOVA is above with $SSR_f = 1389.491$ (df = 2)
 $SSE_f = 348.259$ (df = 17)

Reduced model is $y = \beta_0 + \beta_1 x_1 + \varepsilon$, ANOVA table is below

Rerun the ANOVA (same steps as above, except you will have only one independent variable, "waist").

$SSR_r = 1366.790$ (df = 1)
 $SSE_r = 370.960$ (df = 18)

Model		Sum of Squares	df	Mean Square	F	Sig.
1	Regression	1366.790	1	1366.790	66.320	.000 ^b
	Residual	370.960	18	20.609		
	Total	1737.750	19			

a. Dependent Variable: fat

b. Predictors: (Constant), waist

$$H_0 : \beta_2 = 0 \quad \alpha = 0.05$$

$$H_a : \beta_2 \neq 0$$

$$F_{part} = \frac{[SSR_f - SSR_r] / [df_{SSR_f} - df_{SSR_r}]}{SSE_f / df_{SSE_f}} = \frac{(1389.491 - 1366.790) / (2 - 1)}{348.259 / 17} =$$
$$= \frac{22.701}{20.48582} = \underline{\underline{1.10813}}$$

R.R: we reject H_0 if $F_{part} > F_{\alpha(1,17)} = F_{0.05(1,17)} = 4.45$