

Lecture 18: Indexed Sequential FilesLast Day: B-trees

- Sequential retrieval
- Deletions

Today: B⁺ trees

- Tree structure
- Insertions
- Deletions

Folk & Zoellick, ch. 9
+ handout

B⁺ Trees

B⁺ trees are like B trees except

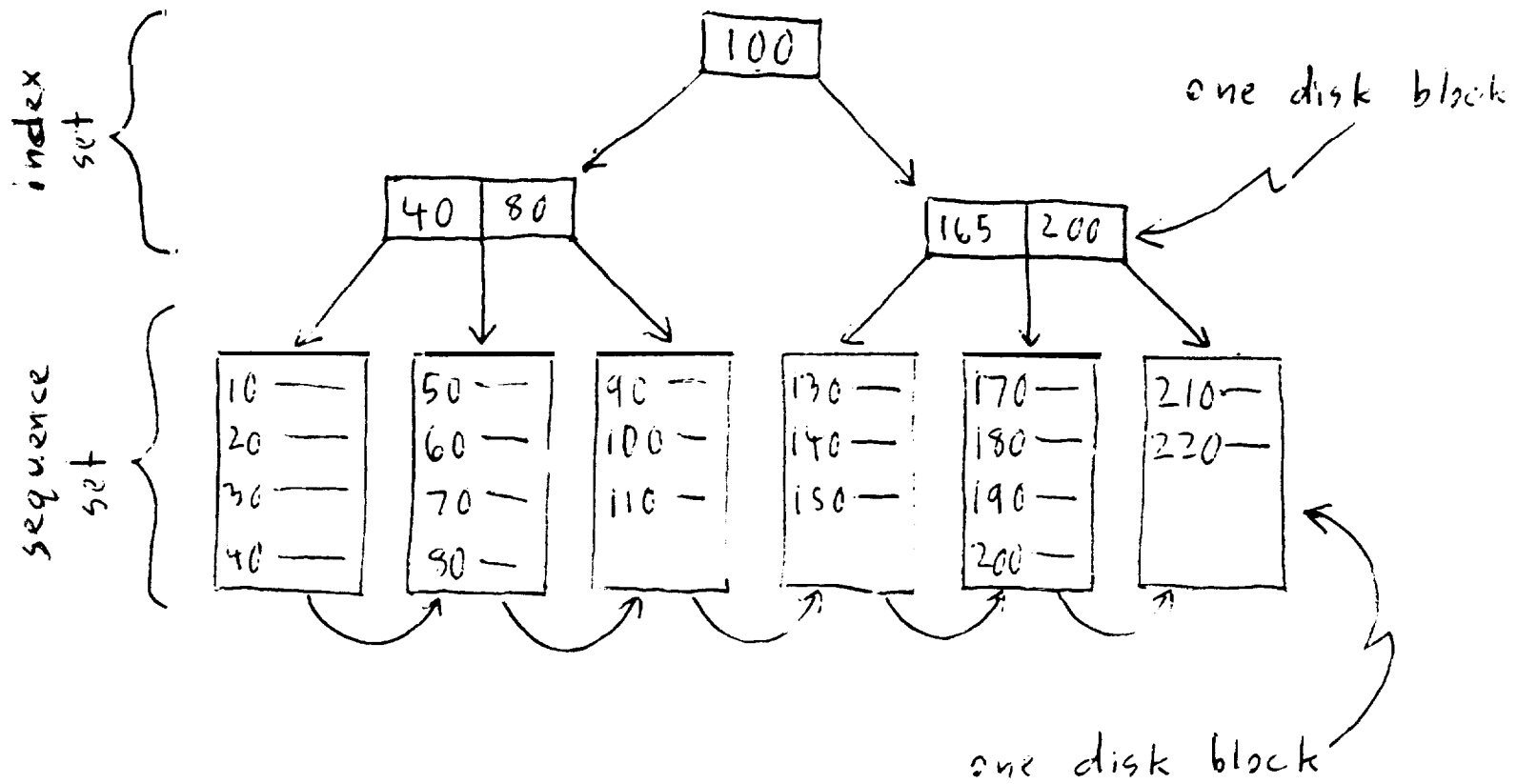
(1) Only leaf nodes contain records.

(2) The leaf nodes are linked together to form a sequence set of data records (for efficient sequential retrieval).

Main Advantages:

- Nodes in a B⁺ tree have many more children than nodes in a B tree.
 - ∴ B⁺ trees are much bushier & shallower than B trees, so retrievals are faster.
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Example of a B⁺ Tree

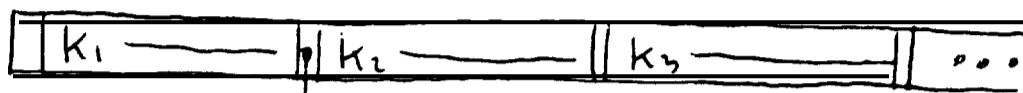


Note:

- Keys may appear more than once (eg, 40, 80, 200).
- Usually, index nodes contain many more keys than leaf nodes.
- Only leaf nodes contain data

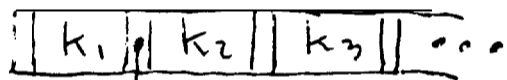
Internal Nodes

B-tree Node:



leads to records with $k_1 < \text{key} < k_2$

B⁺ tree Nodes:



leads to records with $k_1 < \text{key} \leq k_2$

Example

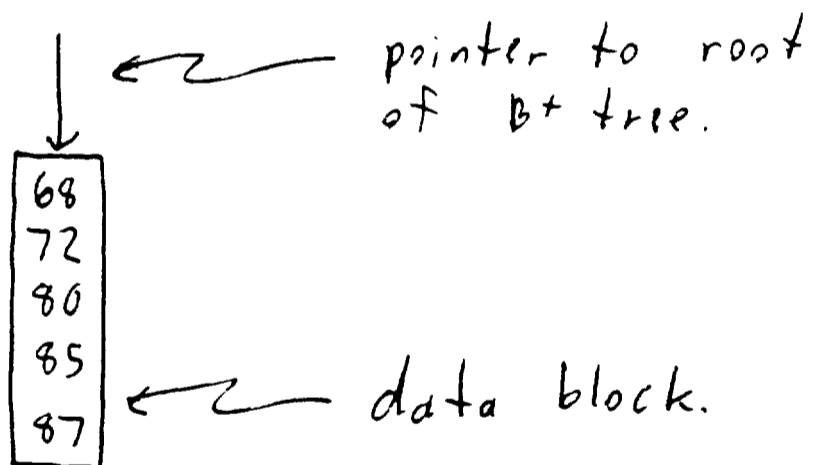
Building a B^+ tree, where

- index nodes have order 3
(can hold 2 keys)

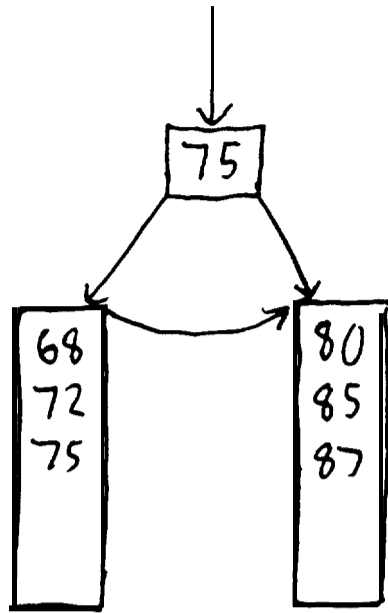
- data blocks can hold 5 records.

Insert records into a tree that is initially empty.

Insert: 68, 72, 80, 85, 87



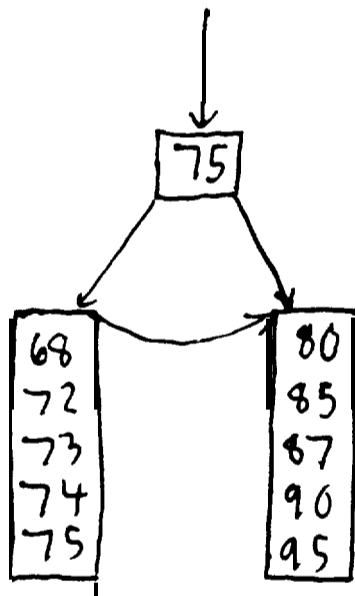
Insert 75:



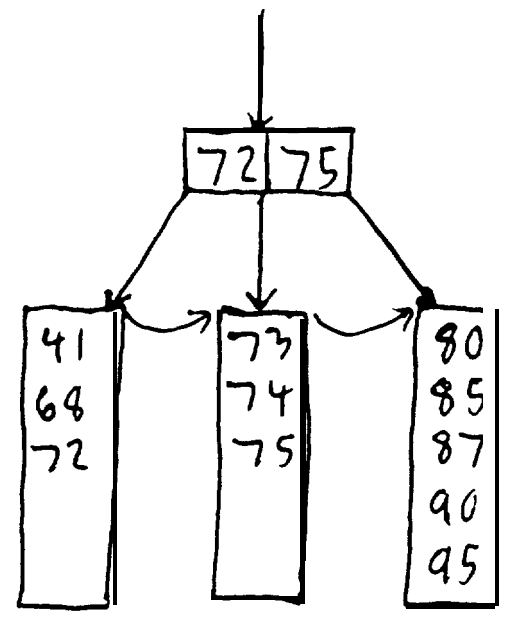
← index node

← data blocks
(sequence set)

Insert: 73, 74, 90, 95



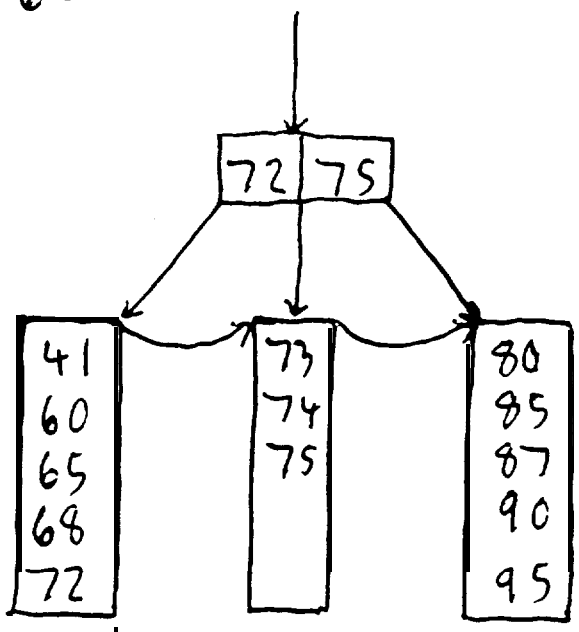
Insert: 41



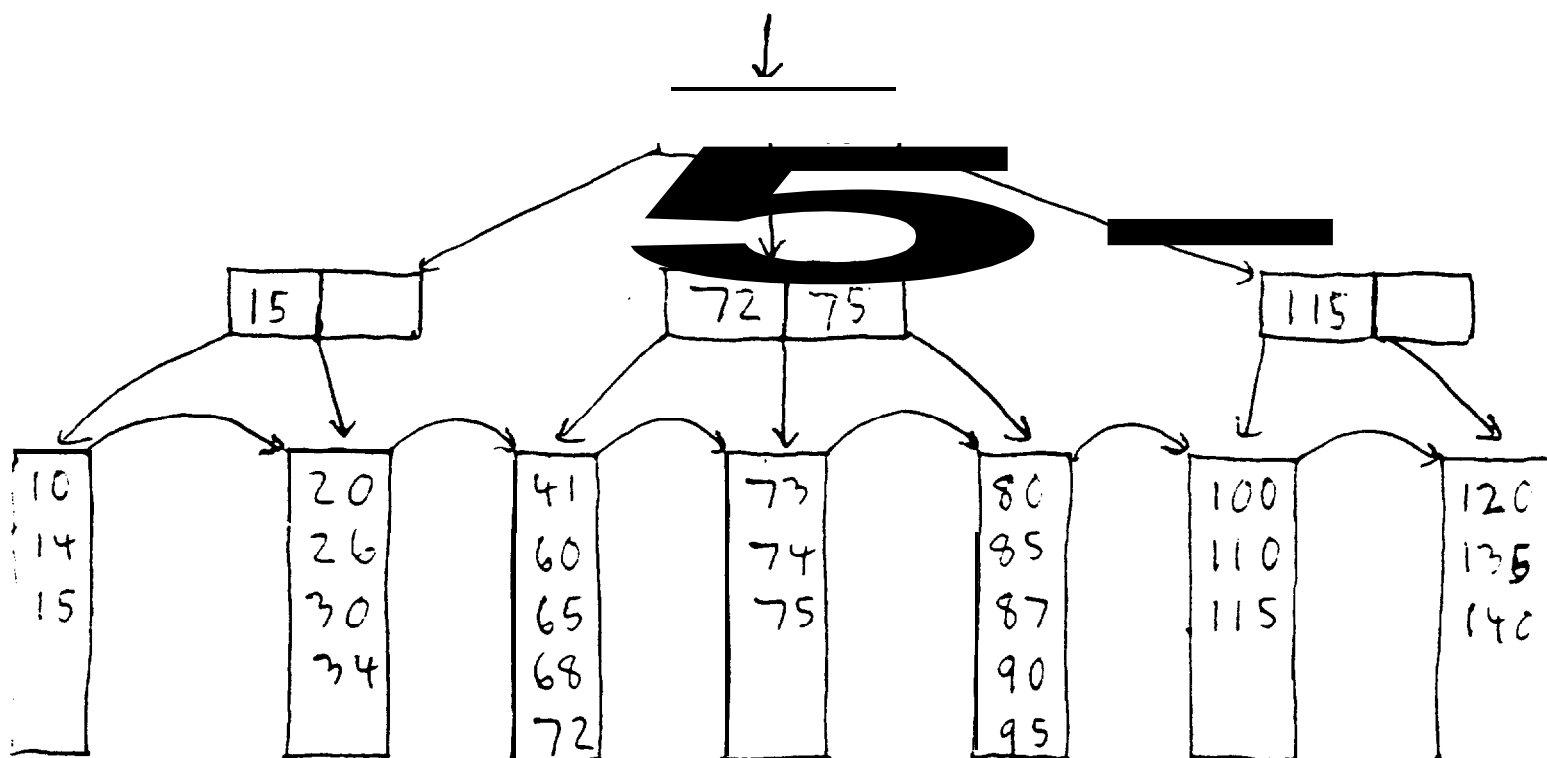
← index node

← data blocks (sequence set)

Insert: 60, 65



A Larger B+ Tree

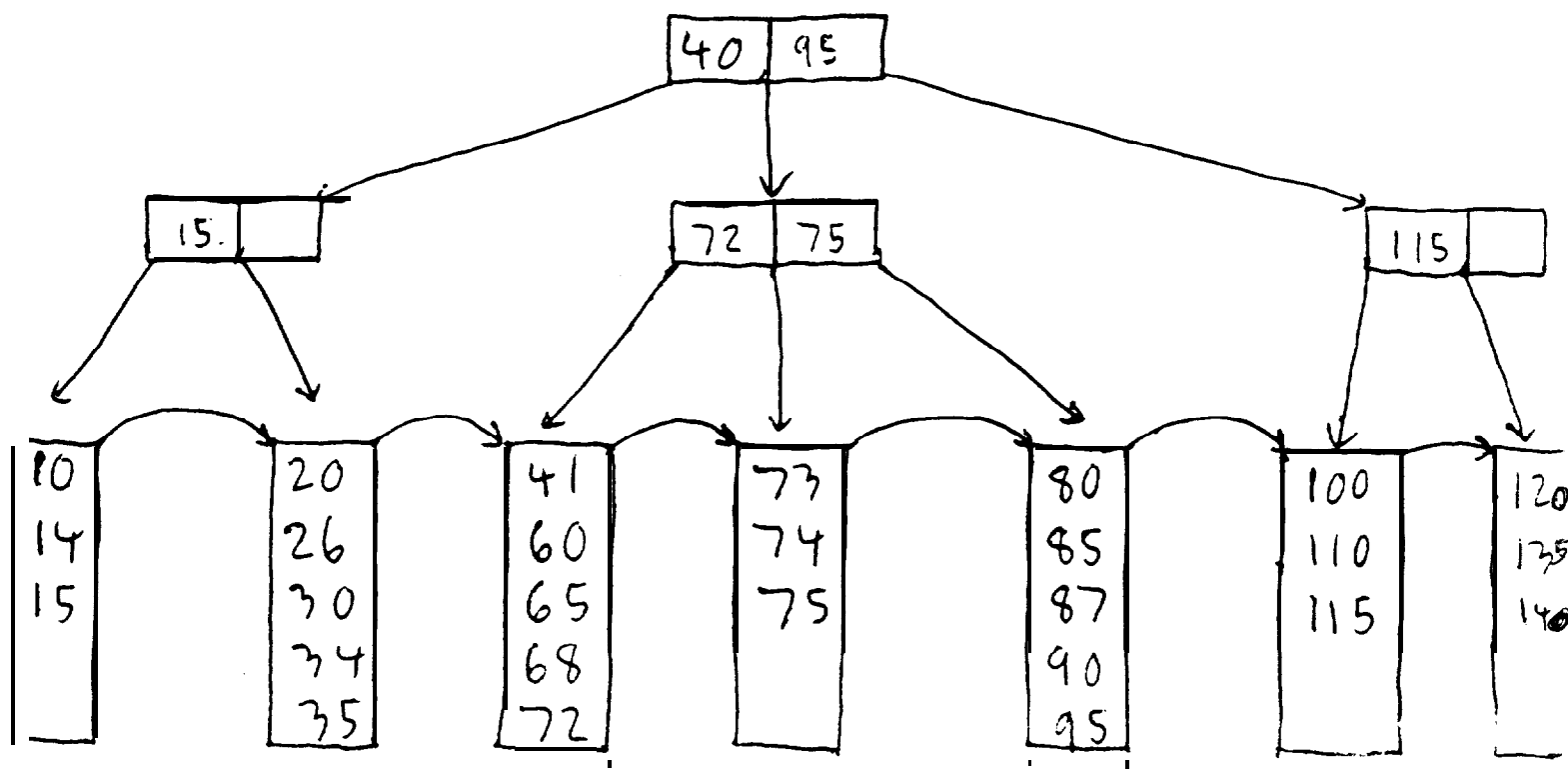


Notes:

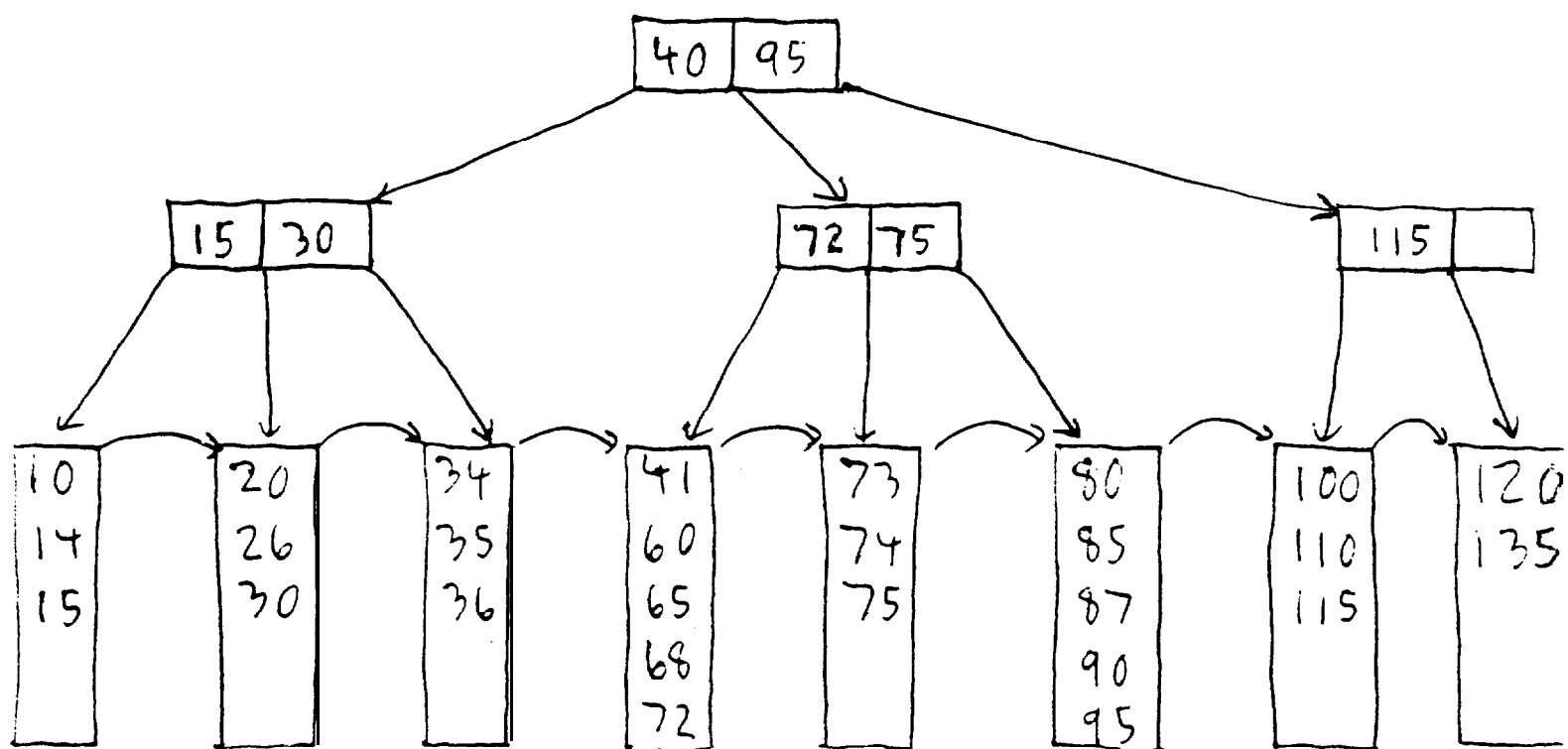
- Index nodes still have order 3
- Leaf nodes can still hold 5 records

Continue to insert records...

eg. insert 35 (easy)



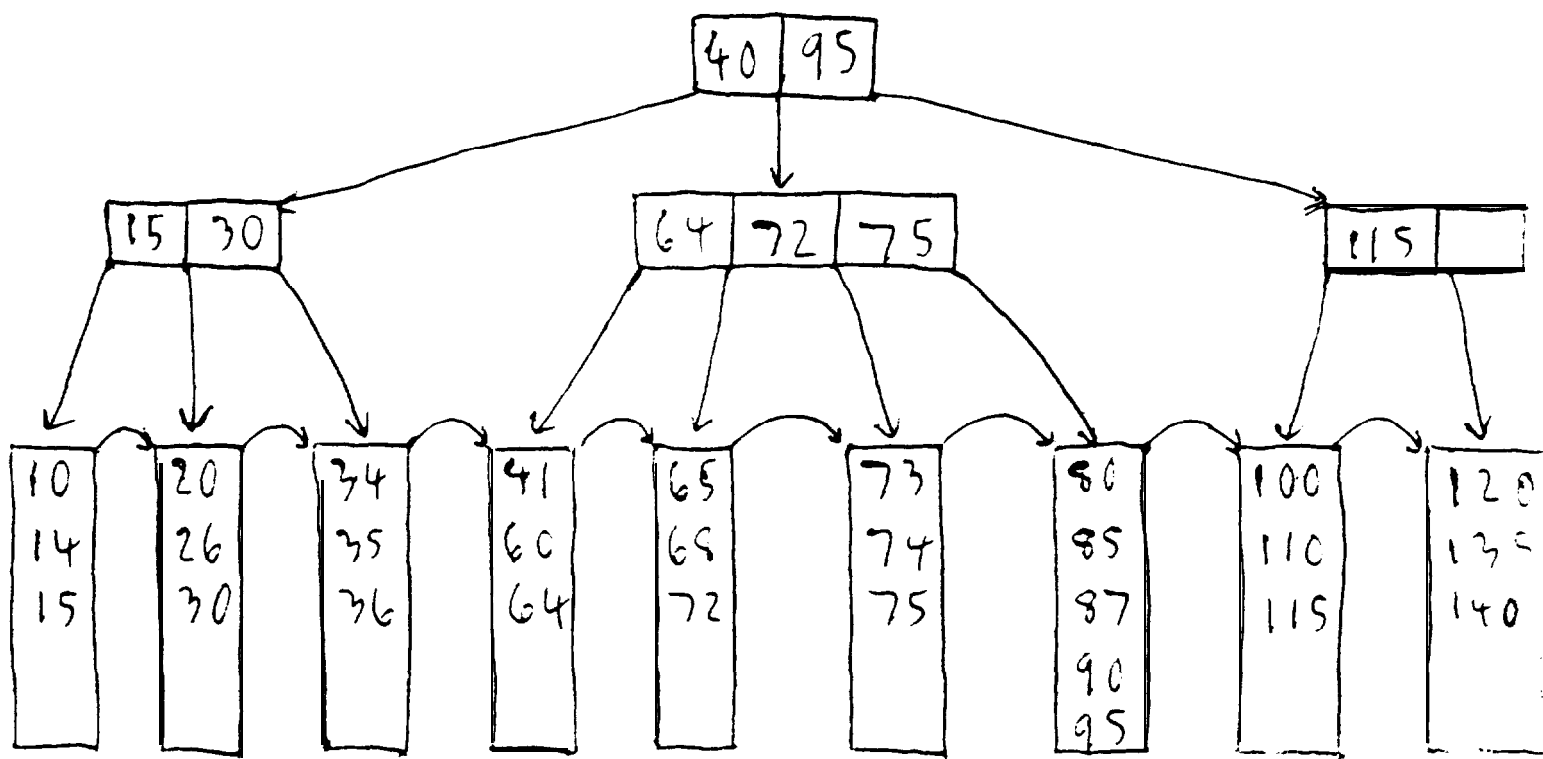
insert 36 (split)



Note: 30 now appears twice,
in a data block, & in an index blk.

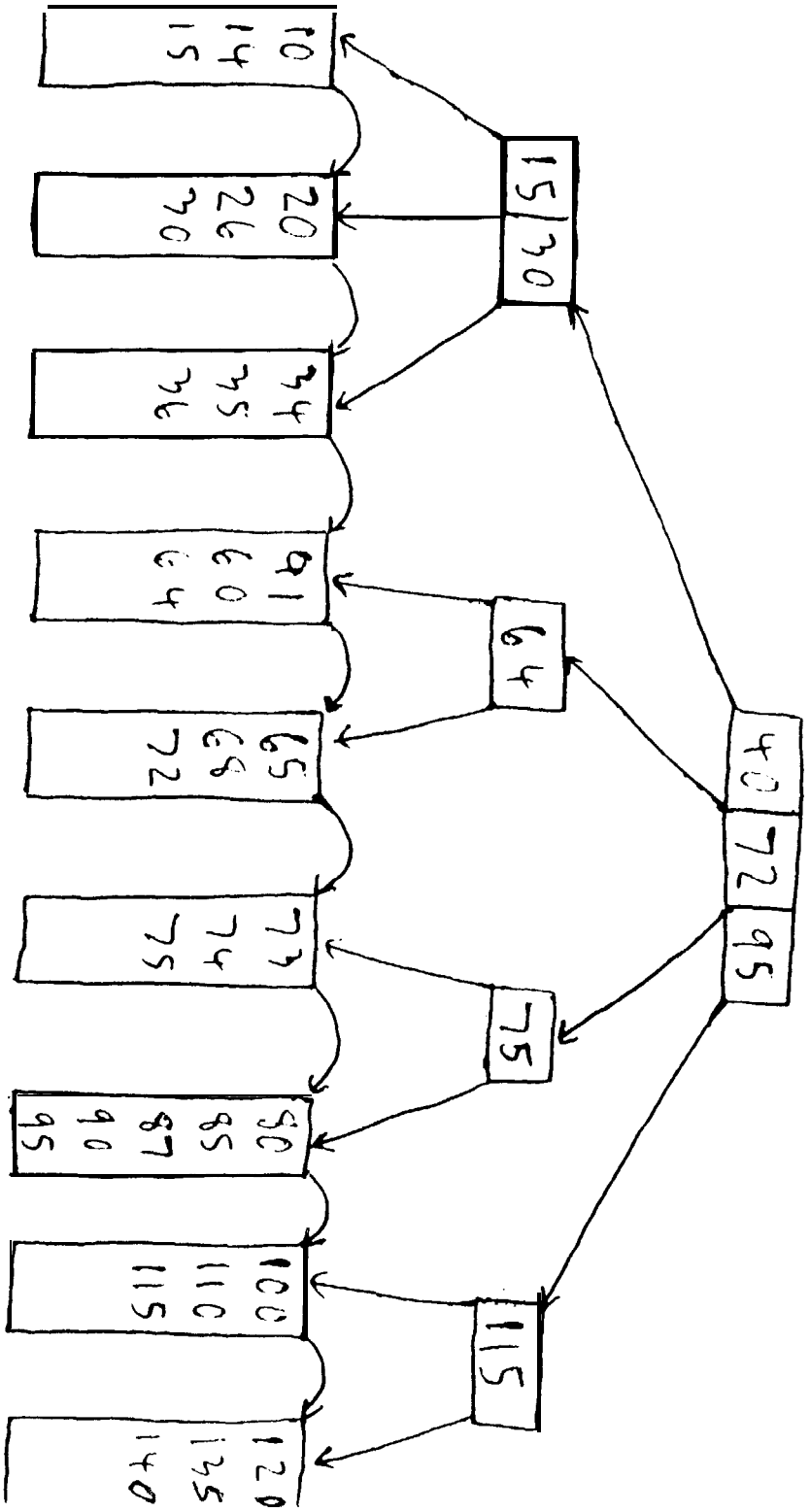
This is a result of splitting a data
blk.

insert 64 (split data block)



Note:

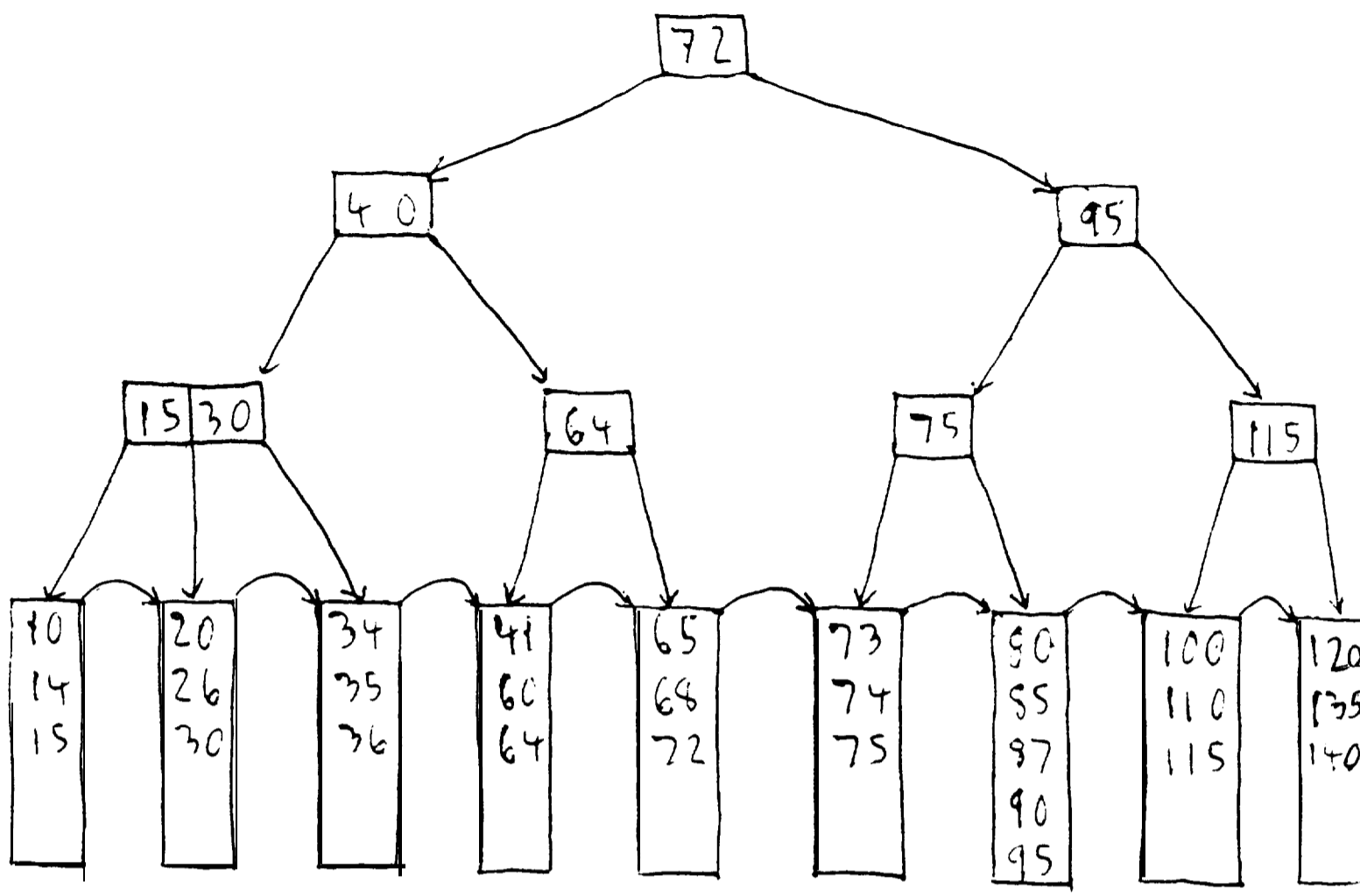
Index node is now too big: Split again.



Note.

Root node is now too big: Shift!





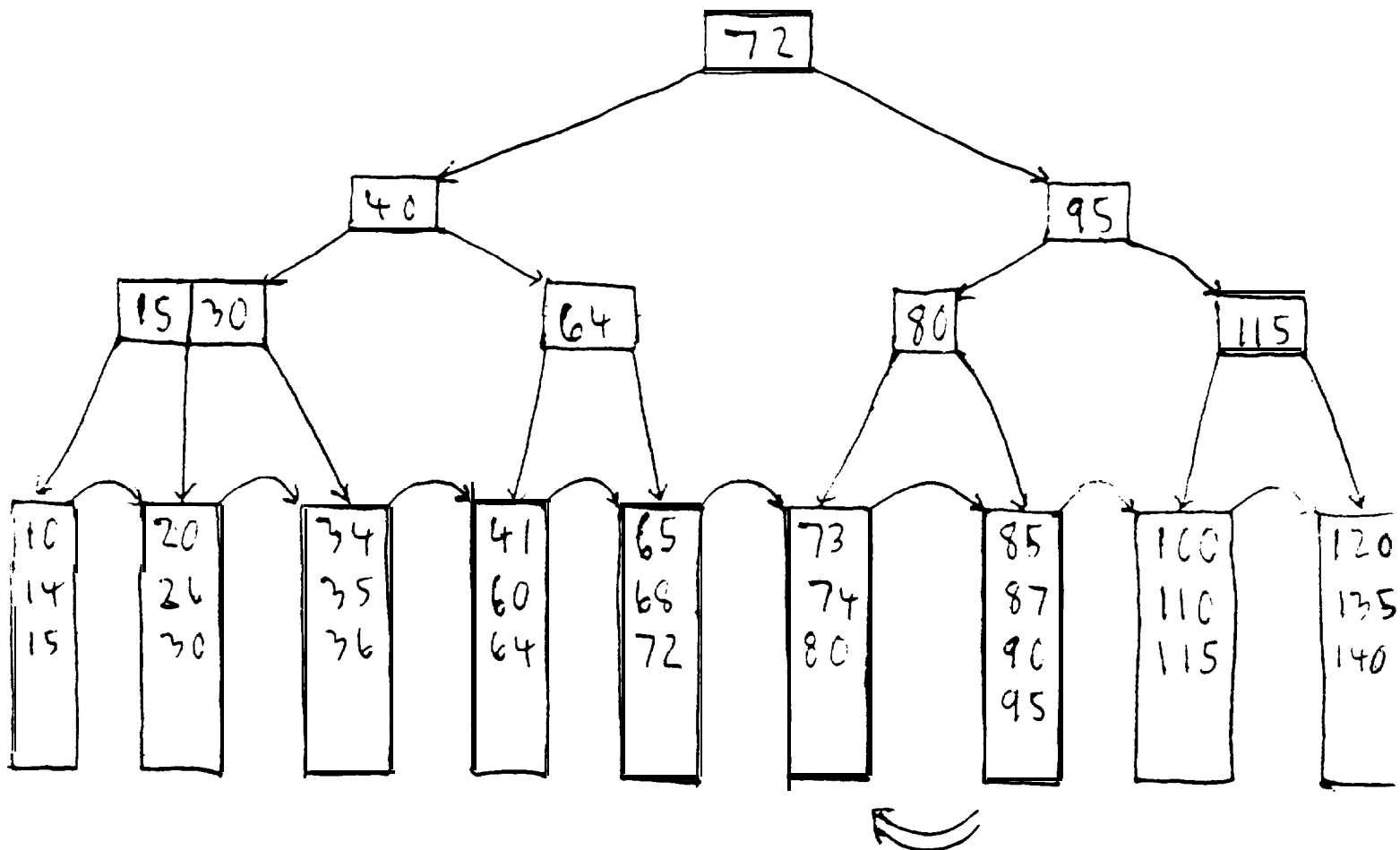
Observe. Splitting of index nodes is just like splitting B-tree nodes. (Only the splitting of data blocks is different).

Deletions From B⁺ Trees

18-14

Unlike B-trees, all deletions in B⁺ trees are from leaves (data blocks),

eg. Delete 75 (Borrow from sibling)



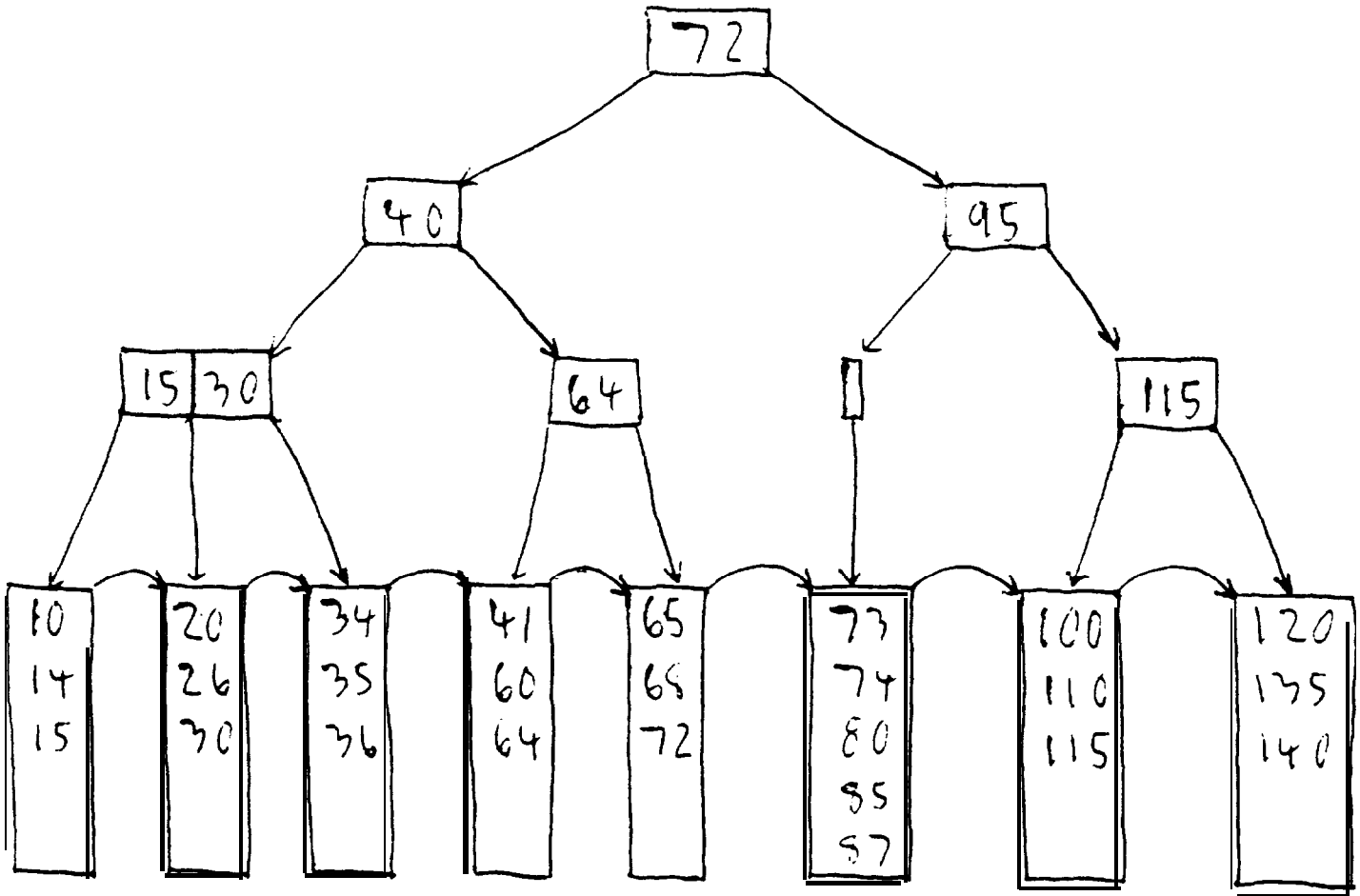
Note: 80 now appears twice, and 75 has disappeared altogether.

Delete 95 (no problem)

Delete 90 (merge)

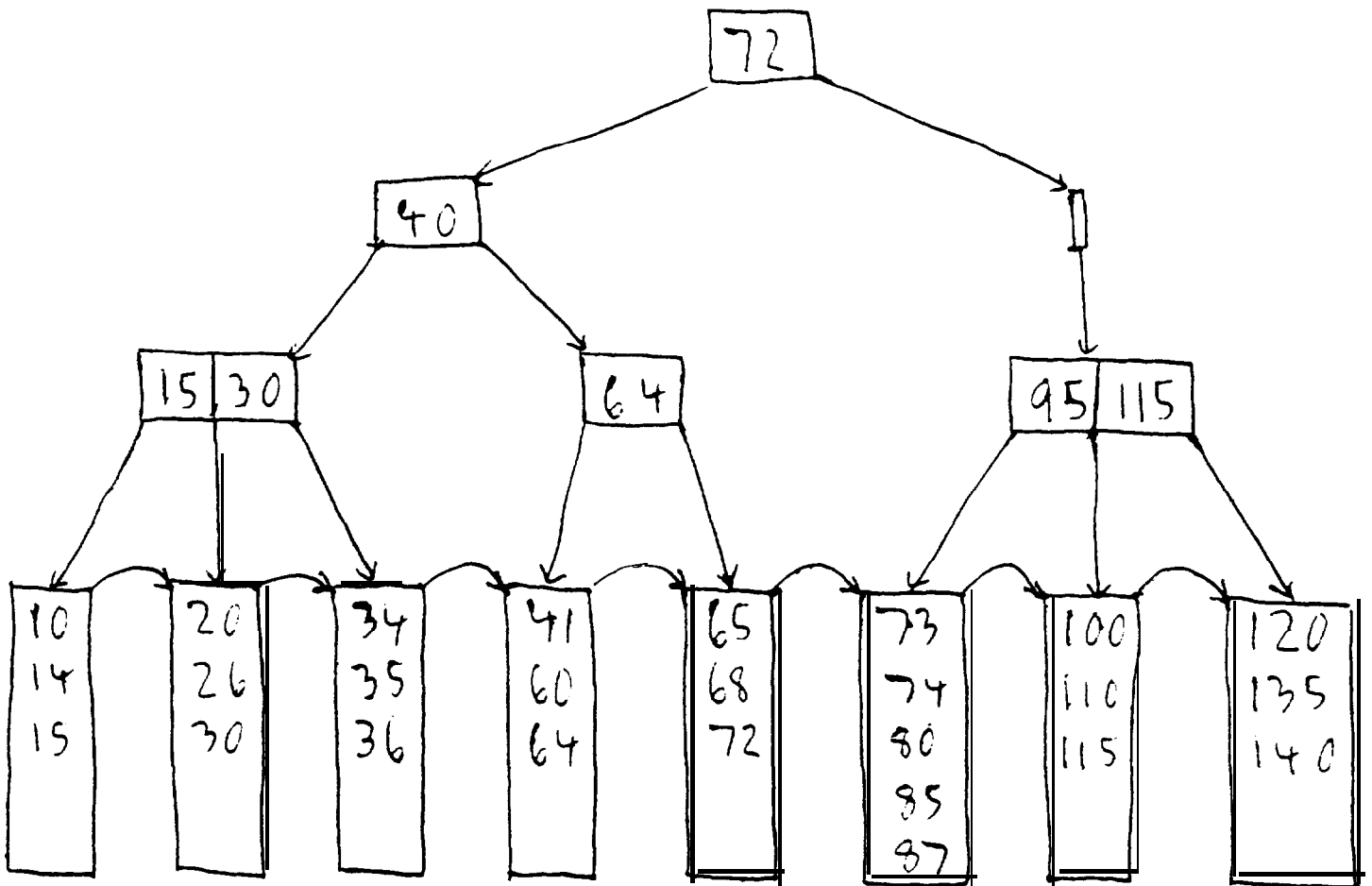
Data block is less than half full.

Merge with sibling.



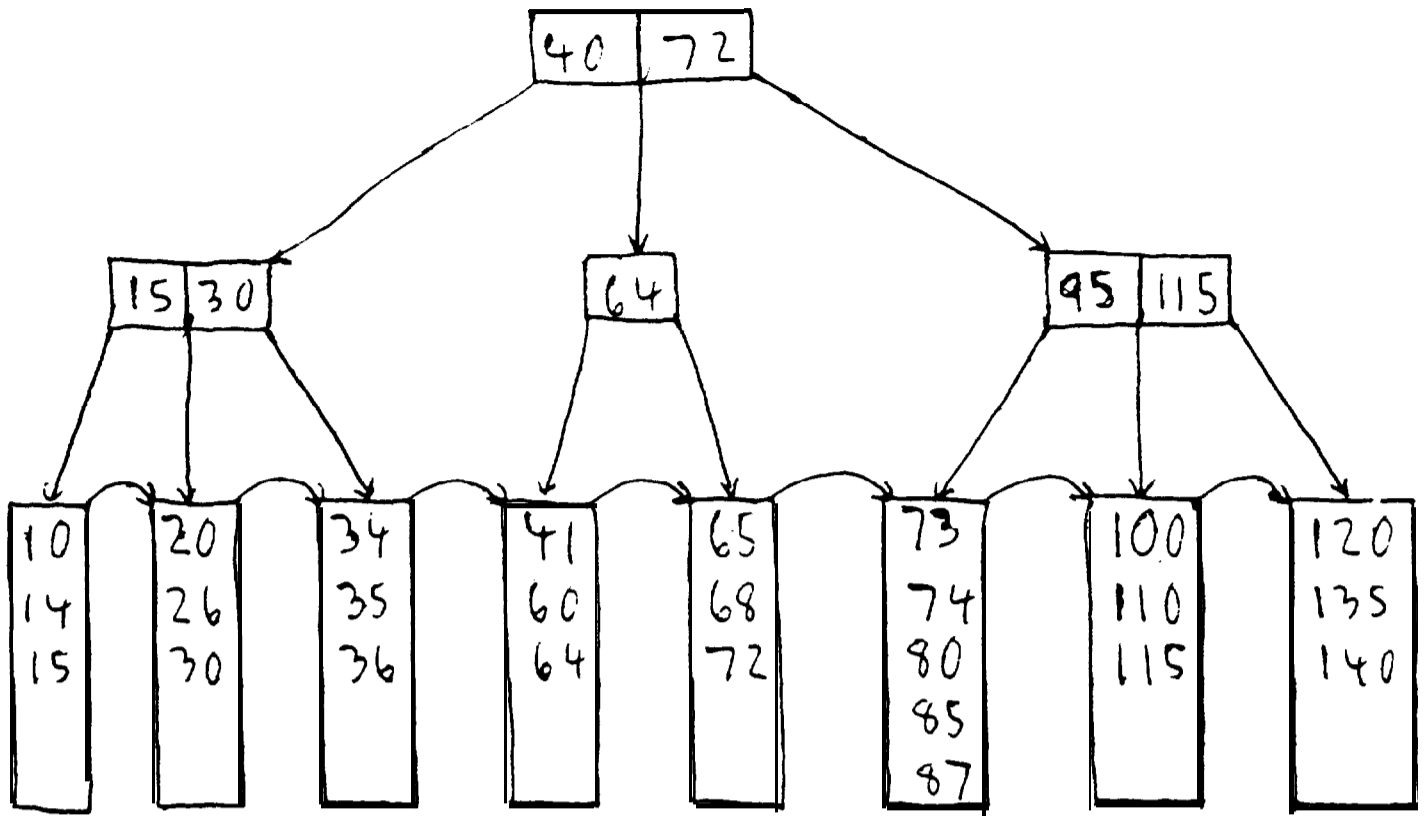
Note: Index node is too small.

Merge with sibling (115).



Note: A higher index node is
now too small.

Merge with sibling (40).



Note. We now have a new root,
one level lower.

Observe: Merging index nodes is just
like merging B-tree nodes.

(Only the merging of data blocks
is different.)

Summary of Indexed Sequential Files

Advantages:

- Sequential retrieval is efficient
- Range queries are efficient
- Retrieving a single record (given its key) is fast (comparable to direct files).

Disadvantages:

- Overhead (i.e., space & maintenance costs) for the index
- Static indexes require off-line reorganization